HIMACHAL PRADESH BOARD OF SCHOOL EDUCATION, DHARAMSHALA

CLASS: XII

SUBJECT : MATHEMATICS (Full Syllabus)

TIME ALLOWED: 3 HOURS

MAX.MARKS:80

(1)

(1)

Special Instructions:

- i. While answering your Questions, you must indicate on your answer-book the same Question No. as appear in your Questions Paper.
- ii. All Questions are compulsory.
- iii. Internal choices have been provided in some questions. Attempt only one of the choices in such questions.
- iv. Do not leave blank page / pages in your answer book.
- Question numbers 1 16 are multiple choice questions (M.C.Q.) carrying 1 mark each.
- vi. Question numbers 17 25 are of 3 marks each.
- vii. Question numbers 26 28 are of 4 marks each.
- viii. Question numbers 29 33 are of 5 marks each.
- ix. Graph paper must be attached in between the answer book.
- Q.1. Let $f: R \to R$ be defined as f(x) = 3x (1) Choose the correct answer:

| (a) f is one-one onto | (b) f is many one onto |
|-------------------------------|-----------------------------------|
| (c) f is one-one but not onto | (d) f is neither one-one nor onto |

Q.2.
$$\tan^{-1}\sqrt{3} - \cot^{-1}(-\sqrt{3})$$
 is equal to (1)

(a) $2\sqrt{2}$ (b) π (c) $-\frac{\pi}{2}$ (d) 0

Q.3. If $\sin^{-1} x = y$ then:

(a) $0 \le y \le \pi$ (b) $-\frac{\pi}{2} \le y \le \frac{\pi}{2}$ (c) $0 < y < \pi$ (d) $-\frac{\pi}{2} < y < \frac{\pi}{2}$

| Q.4. | .4. The number of all possible matrices of order 3×3 with each | | | | | | |
|------|--|--------|-----|----|---------|-----|--|
| | entry 0 or | 1 is: | | | | (1) | |
| | (a) 27 | (b) 18 | (c) | 81 | (d) 512 | | |

- Q.5. The second order derivative of $\log x$ is:
 - (a) $\frac{1}{\chi}$ (b) $\frac{1}{\chi^2}$ (c) $-\frac{1}{\chi^2}$ (d) None of these
- Q.6. The rate of change of the area of the circle with respect to its Radius r = 6 cm is: (1)

(a) 10π cm (b) 12π cm (c) 8π cm (d) 11π cm

Q.7. The approximate change in the volume of a cube of side x meters caused by increasing the side by 3 % is: (1)

(a) $0.09 x^3 m^3$ (b) $0.9 x^3 m^3$ (c) $0.06 x^3 m^3$ (d) $0.6 x^3 m^3$

Q.8. $\int e^x s (1 + t t) d$ equals to: (1) (a) $e^{x}c_{1} + C$ (b) $e^{x}s_{1} + C$ (c) $e^{x}s_{1} + C$ (d) $e^{x}t_{1} + C$ Q.9. Area lying between the curves $y^2 = 4x$ and y = 2x is: (1) (a) $\frac{2}{3}$ (b) $\frac{1}{3}$ (c) $\frac{1}{4}$ (d) $\frac{3}{4}$ Q.10. The order of the differential equation (1) $2x^2 \frac{d^2y}{dx^2} - 3\frac{d}{d} + y = 0$ is: (a) 2 (b) 0 (d) not defined 1 (c) Q.11. The integrating factor of the differential equation (1) $x_{d}^{d} - y = 2x^{2}$ is: (a) e^{-x} (b) e^{-y} (c) x (d) $\frac{1}{x}$

Q.12. If
$$\vec{a}.\vec{b} = |\vec{a}| |\vec{b}|$$
, Then $\theta =$? (1)
(a) $\frac{\pi}{4}$ (b) 0 (c) π (d) $\frac{\pi}{2}$

(1)

Q.13. Direction cosines of z- axis are:

(a) 0, 1, 0 (b) 1, 0, 0 (c) 0, 0, 1 (d) None of these

Q.14. Distance of the plane 2x - y + 2z + 3 = 0 from the point (1) (3, -2, 1) is:

(a)
$$\frac{3}{1}$$
 (b) $\frac{1}{3}$ (c) 0 (d) 13

Q.15. The probability of obtaining an even prime number on each die, (1) when a pair of dice is rolled is:

(a) $\frac{1}{3}$ (b) $\frac{1}{3}$ (c) $\frac{1}{1}$ (d) 0

- Q.16. If A and B are events such that P(A/B) = P(B/A), Then: (1)
 - (a) A B but A B (b) A = B (c) A B = (d) P(A) = P(B)

Q.17. Find gof and fog, if

f(x) = |x| and g(x) = |5x - 2|

Q.18. Using elementary transformations, find the inverse of (3)

 $\begin{bmatrix} 3 & 1 \\ 5 & 2 \end{bmatrix}$

Q.19. Using the properties of the determinants, show that (3)

$$\begin{vmatrix} y+k & y & y \\ y & y+k & y \\ y & y & y+k \end{vmatrix} = k^2 (3y+k)$$

Q.20. Find the value of k so that the function f defined by (3)

$$f(x) = \begin{cases} k + 1, i & x \\ \cos x, i & x > \pi \end{cases}$$
 is continuous at point x = π

- Q.21. Evaluate x l c 2x d (3)
- Q.22. By using the properties of the definite integrals, evaluate (3)

$$\frac{\frac{\pi}{2}}{0} \frac{c}{s} \frac{5x}{5x+c} \frac{5x}{5x} d$$

Q.23. Solve the differential equation:

$$(x^2 - y^2)d + 2xy d = 0$$

OR

Solve the differential equation:

$$x\log x \frac{d}{d} + y = \frac{2}{x}\log x$$

- Q.24. Two cards are drawn at random and without replacement from a pack of 52 playing cards. Find the probability that both the cards are black. (3)
- Q.25. Find the probability distribution of number of tails in the simultaneous tosses of 3 coins. (3)

OR

Find the probability of getting 5 exactly twice in 7 throws of a die.

Q.26. Prove that

(4)

(3)

(3)

$$\tan^{-1}\frac{2}{1} + \tan^{-1}\frac{7}{2} = \tan^{-1}\frac{1}{2}$$

OR

Express $\tan^{-1}\left(\frac{x}{a^2-x^2}\right), |x| < a$ in the simplest form:

Q.27. Differentiate
$$sin\{tan^{-1}(e^x)\}$$
 with respect to x. (4)

OR

If
$$y^x = x^y$$
, find $\frac{d}{d}$

Q.28. Find the area of a parallelogram whose adjacent sides are determined by the vectors. (4)

$$\vec{a} = \imath - \jmath + 3\hat{k}$$
 and $\vec{b} = 2\imath - 7\jmath + \hat{k}$

Q.29. Solve the system of linear equations, using matrix method. (5)

$$x - y + z = 4$$

2x + y - 3z = 0
X + y + z = 2

Q.30. Find two positive numbers x and y such that x + y = 60 and Xy^3 is maximum. (5)

OR

Find the equation of tangent and normal to the parabola

 $y^2 = 4ax$ at point (at², 2at)

Q.31. Find the area of the region bounded by the ellipse

OR

$$\frac{x^2}{4} + \frac{y^2}{9} = 1$$

Using integration find the area of region bounded by the triangle whose vertices are (-1,0), (1,3) and (3,2)

Q.32. Find the shortest distance between the lines

(5)

(5)

$$\vec{r} = (\iota + 2j + \hat{k}) + (\hat{\iota} - j + \hat{k})$$

$$\vec{r} = (2\iota - j - \hat{k}) + \mu(2\hat{\iota} + j + 2\hat{k})$$

OR

Find the equation of plane through the intersection of the planes 3x - y + 2z - 4 = 0 and x + y + z - 2 = 0 and passes through the point (2, 2, 1).

Q.33. Solve the following linear programming problem (LPP) graphically: Maximize Z = 5x + 3y subject to the constraints (5)

> 3x + 5y 15 5x + 2y 10 x 0 y 0